



Fractions

Multiplication: Multiply the fraction straight across with numerator times numerator and denominator times denominator.

Ex.

$$\frac{3}{6} \times \frac{5}{2} = \frac{3 \times 5}{6 \times 2} = \frac{15}{12}$$

Division: To divide fractions we can flip the second fraction and turn the problem into a multiplication problem.

Ex.

$$\frac{5}{8} \div \frac{3}{2} = \frac{5}{8} \times \frac{2}{3} = \frac{10}{24}$$

Addition & Subtraction: We need to have a common denominator to add and subtract fractions.

Ex.

$$\begin{aligned} \frac{x}{5} - \frac{x}{10} &= \frac{x}{5} \left(\frac{2}{2} \right) - \frac{x}{10} \\ &= \frac{2x}{10} - \frac{x}{10} \\ &= \frac{2x - x}{10} = \frac{x}{10} \end{aligned}$$

Simplification: To simplify fractions, write out the prime factorization of each number and cancel out any prime factors that are present in the top and bottom of the fraction.

Ex.

$$\frac{24}{45} = \frac{2 \times 2 \times 2 \times \cancel{3}}{\cancel{3} \times 3 \times 5} = \frac{8}{15}$$

Ratios

All ratios can be rewritten as a fraction. Add the numbers of the ratio to get the denominator and use the individual numbers as numerators.

Ex.

For a recipe the ratio of water to flour for is 2:3.

$$2 + 3 = 5$$

What fraction is water?

$$\frac{2}{5}$$

What fraction is flour?

$$\frac{3}{5}$$

Sequence of Operations

Please

Excuse

My Dear

Aunt Sally

Parentheses ()

Exponents ²

Multiplication and Division $\times \div$

Addition and Subtraction $+$ $-$

Units of Measurement

Imperial

Length:

1 foot (ft.) = 12 inches (in.)

1 yard (yd.) = 3 ft.

1 mile (mi.) = 1760 yd. = 5280 ft.

Volume:

1 cup (c.) = 8 fluid ounces (fl. oz.)

1 quart (qt.) = 2 c.

1 pint (pt.) = 2 qt.

1 gallon (gal.) = 2 pt.

Weight:

1 pound (lb.) = 16 ounces (oz.)

1 ton (t.) = 2240 lb.

Metric

kilo- 1,000 Thousand

hecto- 100 Hundred

deca- 10 Ten

(base) 1 One

deci- .1 Tenth

centi- .01 Hundredth

milli- .001 Thousandth

Length:

Meter (m)

Volume:

Liter (l)

Weight:

Gram (g)

Conversions between Metric and Imperial:

1 in. \approx 2.5 cm (\approx diameter of quarter)

1 mi \approx 1.6 km

1 qt. \approx 1 l

1 oz. \approx 28 g (\approx weight of 5 quarters)

2.2 lbs. \approx 1 kg (\approx weight of a dictionary)

Exponents

An exponent represents the number of times the base is multiplied by itself.

Ex. $2^3 = 2 \times 2 \times 2 = 8$

Any number to the 0 exponent equals

1

Ex. $2^0 = 54^0 = 13^0 = 1$

Negative exponents can be rewritten as fractions with positive exponents.

Ex. $4^{-2} = \frac{1}{4^2} = \frac{1}{16}$

Exponent Operations

Add the exponents when multiplying the same base.

Ex. $3^4 \times 3^5 = 3^9$

Subtract the exponents when dividing the same base.

Ex. $\frac{6^8}{6^3} = 6^5$

When a base with an exponent is raised to another exponents, multiply the exponents together.

Ex. $(3^4)^5 = 3^{20}$



Roots

A root is the opposite of an exponent. When given an expression like $\sqrt{9}$, think about what number squared is equal to 9. That is $x^2 = 9$, thus $\sqrt{9} = 3$.

Whenever you have only the radical, $\sqrt{\quad}$, that means the square roots. Any other root will index the number on the radical, such as $\sqrt[3]{64}$. This is asking for the cube root of 64 which we can think of as $x^3 = 64$, so $\sqrt[3]{64} = 4$.

Translating words to

Numbers

Phrases of Addition:

- Increased by
- Sum of
- More than
- Exceeds by

Phrases of Subtraction:

- Decreased by
- Difference of
- Less/fewer than
- Diminished by

Phrases of Multiplication:

- Times
- Times the
- Sum/Difference
- Product of

Phrases of Equals

- Is
- Result is
- Results in

Ex.

Find the number to make the sentence true:

Three times the difference of a number and seven is fifteen.

$$3 \times (x - 7) = 15$$

$$3(x - 7) = 15$$

$$3x - 21 = 15$$

$$3x = 36$$

$$x = 12$$

Geometry

It is more important to understand the principles of geometry and how 2D and 3D shapes relate to one another than to memorize a formulas, because this test is notorious for coming up with new shapes that you haven't seen before in a practice test.

Area is two-dimensional (2D) meaning that to find the area of something you generally multiple something by something.

Square (S x S) or Rectangle (L x W);

Triangle (1/2 L x W) because a triangle is half a square/rectangle.



Area of circle is (πr^2) therefore $r \times r$ (and always multiple by π for a circle)

Volume is three-dimensional (3D) meaning that to find the volume of something you generally multiple the area of the base times the height.

Cube is (S x S) x H; Cylinder (πr^2) x H

Three pyramids can fit into a cube therefore you multiple the cube volume times 1/3 to get the volume of a pyramid 1/3 (S x S) x H

Three cones can fit into a cylinder therefore you multiple the cylinder volume times 1/3 to get the volume of a cone 1/3 (πr^2) x H